

Semiconductors

1. What is the concentration of free electrons and holes [$\#/cm^3$] of intrinsic silicon at 100K and 310K?

@100K: $p = n = n_i = 7.3 \times 10^{15} (100^{3/2}) \exp(-1.12 / (2 \cdot 8.62 \times 10^{-5} \cdot 100)) = 4.4596 \times 10^{-10}$ (essentially zero)

@310K: $p = n = n_i = 7.3 \times 10^{15} (310^{3/2}) \exp(-1.12 / (2 \cdot 8.62 \times 10^{-5} \cdot 310)) = 3.15 \times 10^{10} \text{ [#}/cm^3]$

2. What is the conductivity and resistivity of intrinsic silicon at 100K and 310K?

@100K: $\sigma =$ essentially zero, $\rho =$ infinity [$\Omega \text{ cm}$]

@310K: $\sigma = 9.24 \times 10^{-6} \text{ [1}/(\Omega \text{ cm})]$, $\rho = 1.082 \times 10^5 \text{ [}\Omega \text{ cm]}$

3. A cylindrical resistor is constructed from intrinsic silicon at 310K having dimensions of radius=0.1cm and length 0.5cm. What is the value of the resistor?

@310K: $R = 0.5 \cdot 1.082 \times 10^5 / (\pi \cdot 0.1^2) = 1.72 \text{ M}\Omega$

4. Repeat 1-3 with doped silicon $N_D = 1 \times 10^{16} \text{ [#}/cm^3]$. (just for 310K)

@310K: $n = 1 \times 10^{16} \text{ [#}/cm^3]$, $p = 1 \times 10^4 \text{ [#}/cm^3]$, $\sigma = 2.16 \text{ [1}/(\Omega \text{ cm})]$, $\rho = 0.46 \text{ [}\Omega \text{ cm]}$, $R = 7.36 \text{ }\Omega$

5. Repeat 1-3 with doped P-type silicon $N_A = 1 \times 10^{16} \text{ [#}/cm^3]$. (just for 310K)

@310K: $p = 1 \times 10^{16} \text{ [#}/cm^3]$, $n = 1 \times 10^4 \text{ [#}/cm^3]$, $\sigma = 0.77 \text{ [1}/(\Omega \text{ cm})]$, $\rho = 1.30 \text{ [}\Omega \text{ cm]}$, $R = 20.72 \text{ }\Omega$

6. The distribution of free electrons in a N-type Silicon with at room temperature is given by the equation (use free electron mobility=2000 cm^2/Vs and $V_T=0.025V$).

$$n(x)|_{t=0} = 1 \times 10^{16} (\cos(2\pi 100x) + 1) \text{ [#}/cm^3], \text{ where } x \text{ is in units of cm.}$$

What is the diffusion current density as a function of position (x) at $t=0$?

$$D_n = 2000 \cdot 0.025 = 50 \text{ cm}^2/s$$

$$J_n = q \cdot D_n \cdot n'(x) = 1.6 \times 10^{-19} [\text{Coulombs}] \cdot 50 [\text{cm}^2/s] \cdot (d/dx) 1 \times 10^{16} (\cos(2\pi 100x) + 1) \text{ [#}/cm^3] [1/cm]$$

$$J_n = 1.6 \times 10^{-19} \cdot 50 \cdot 2\pi 100 \times 10^{16} \cdot (-\sin(2\pi 100)) [\text{Coulombs}] [\text{cm}^2/s] \text{ [#}/cm^3] [1/cm]$$

$$J_n = -16\pi \sin(2\pi 100) [\text{Coulombs}/\text{cm}^2 \cdot s] \text{ or } [\text{Amps}/\text{cm}^2]$$