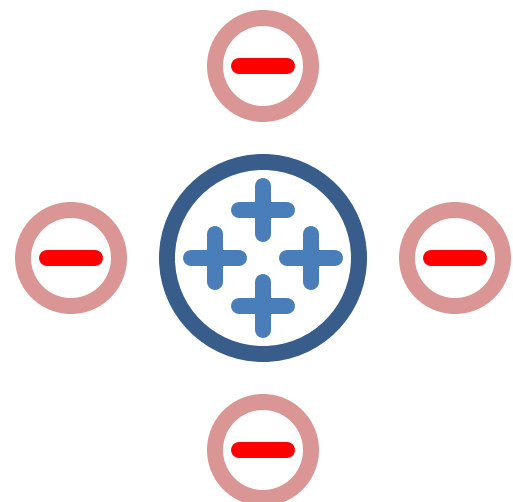
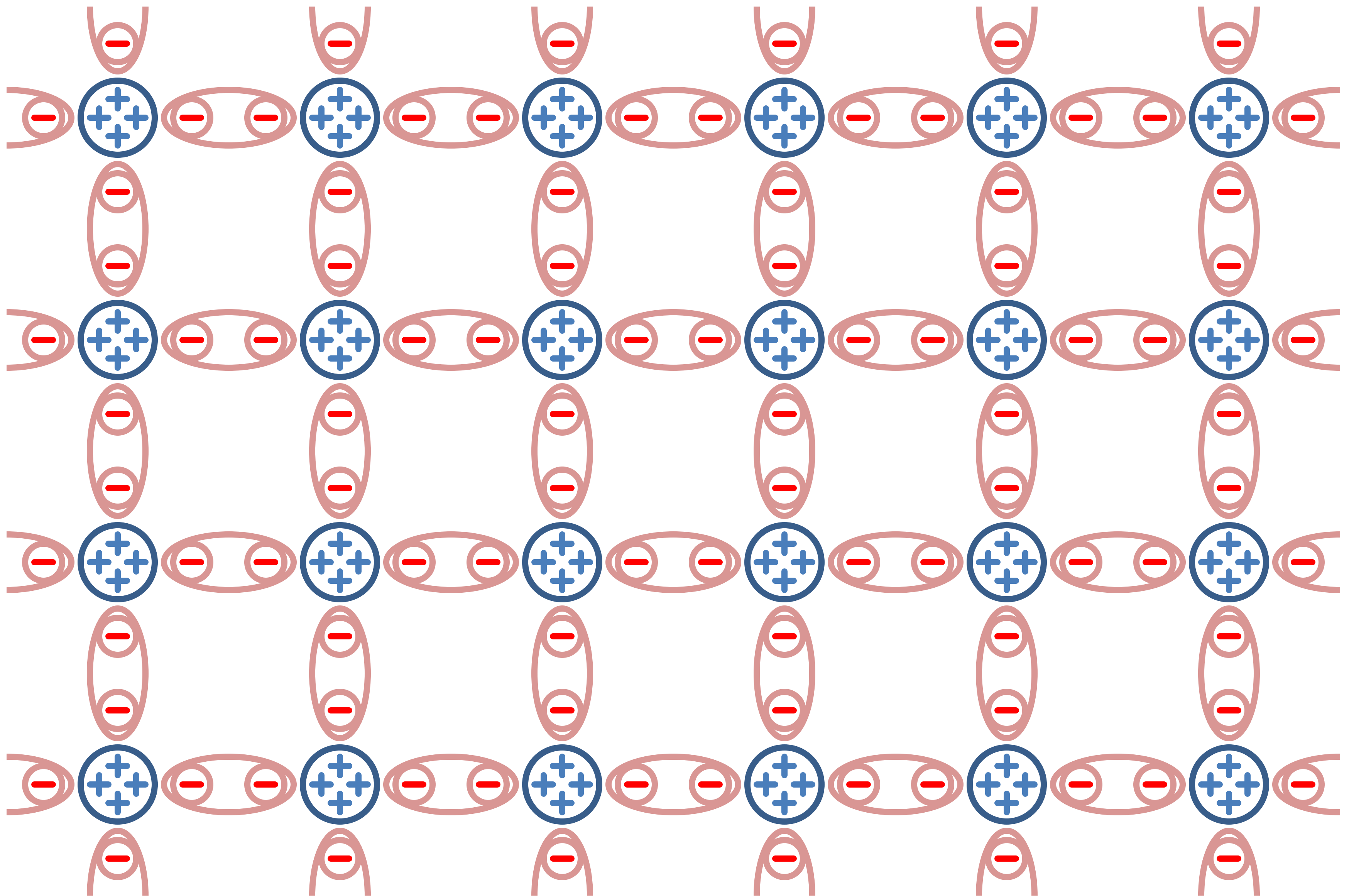




Silicon: **14 electrons**
4 in outer shell

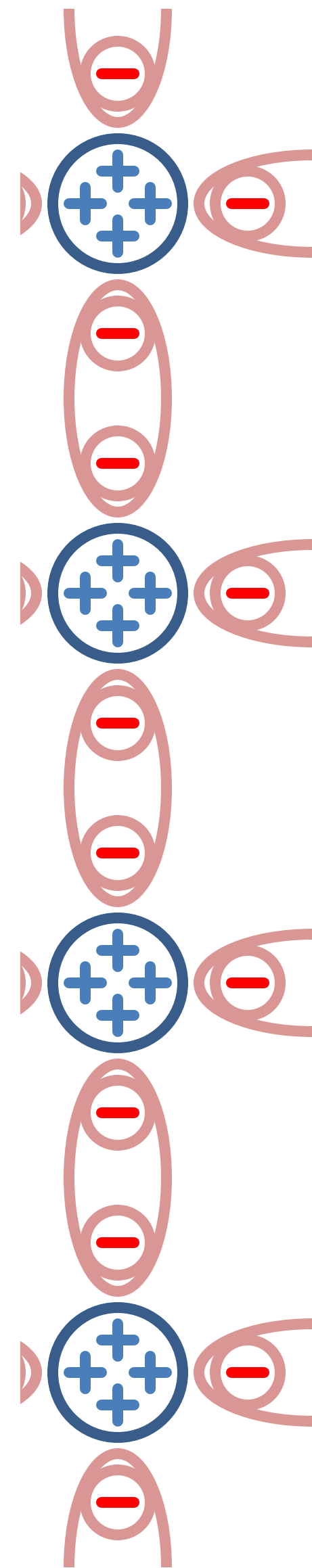
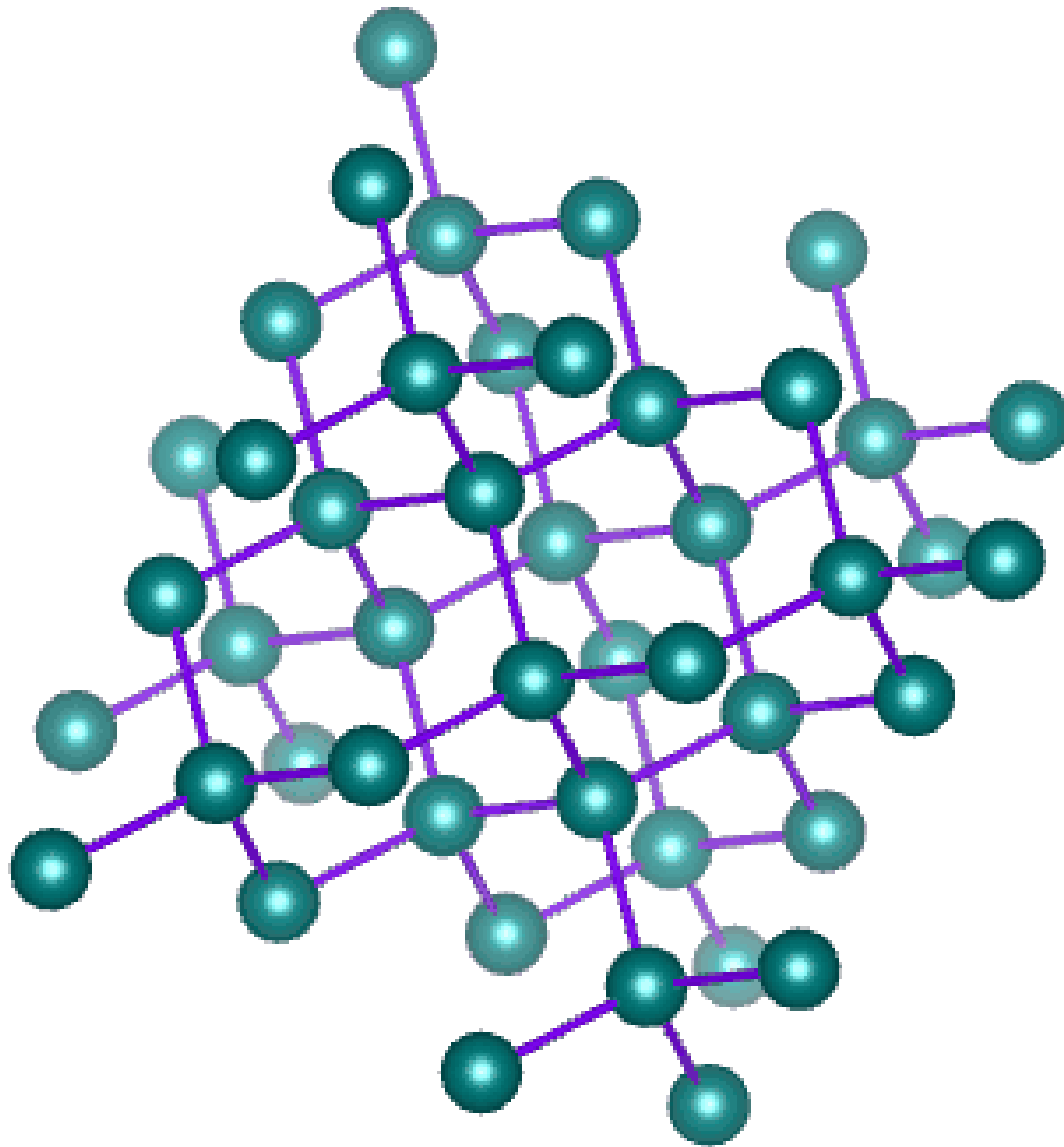
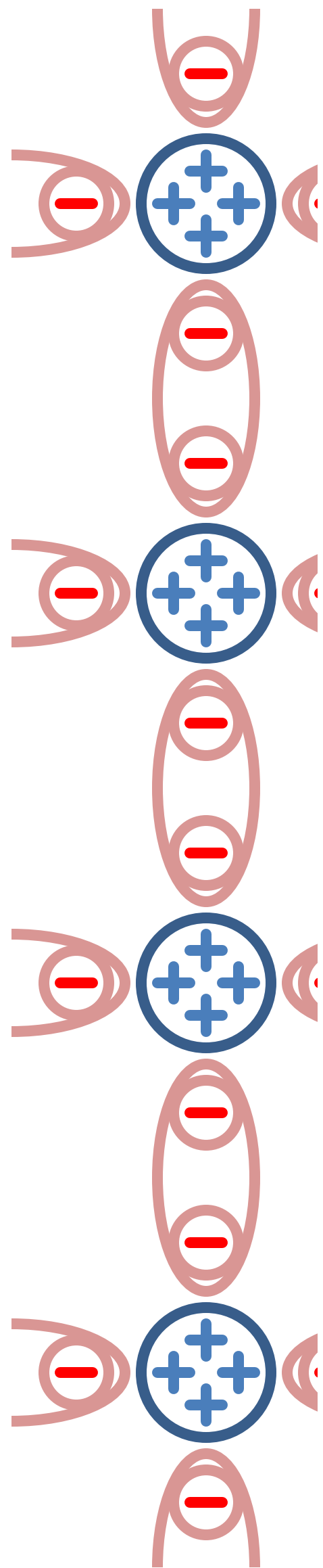
Silicon at T=0K;

Covalent bonds
Poor conductor

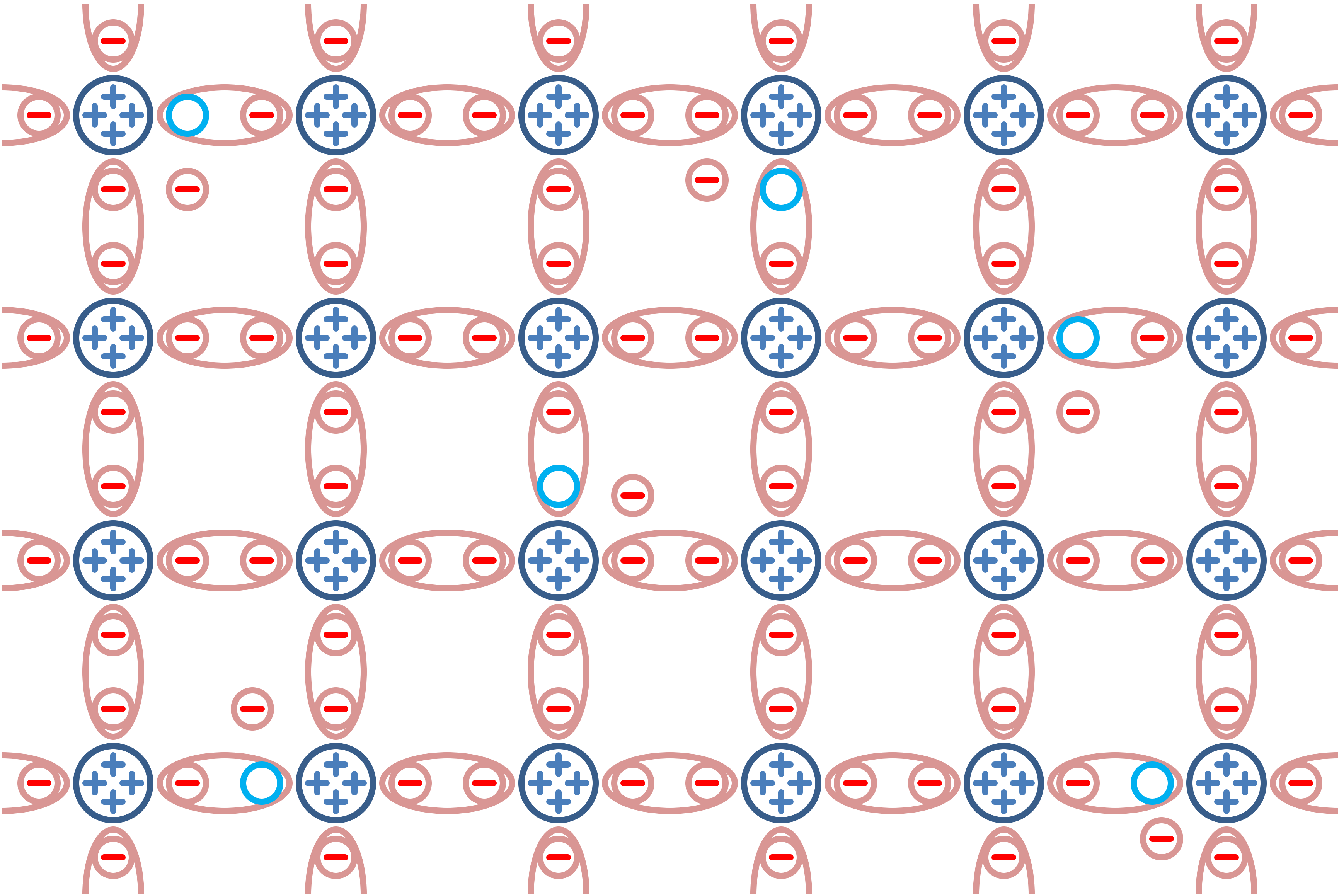


Silicon at $T=0\text{K}$;

**Covalent bonds
Poor conductor**



Silicon at $T > 0\text{K}$; free electrons (f.e.) and holes



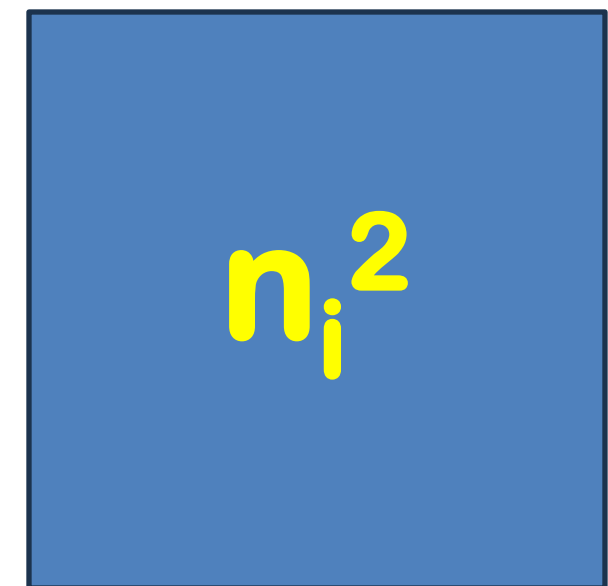
Silicon at $T > 0K$; Better Conductor

Charge Carriers: free electrons and holes

n : number of f.e. per unit volume (cm^3)

p : number of holes per unit volume

$$p = n_i$$



$$n = n_i$$

Intrinsic (pure silicon)

$$n = p = n_i$$

$$n_i = B T^{3/2} e^{-E_g/2kT}$$

$$B = 7.3 \times 10^{15} [\text{cm}^{-3} \text{K}^{-3/2}]$$

$$E_g = 1.12 [\text{eV}], \quad k = 8.62 \times 10^{-5} [\text{eV/K}]$$

Commonly refer to the product

$$pn = n_i^2$$

Area (n_i^2) is set by temperature.

of charge carriers is set by the perimeter.

Square is the worst shape to maximize perimeter ($p+n$).

Silicon at $T > 0\text{K}$; Better Conductor

What is the concentration of charge carriers (p and n) for intrinsic silicon at 27 degree C.

Silicon at $T > 0\text{K}$; Better Conductor

What is the concentration of charge carriers (p and n) for intrinsic silicon at 27 degree C.

$$27\text{C} = 300\text{K}$$

$$p=n=n_i=BT^{3/2}e^{-E_g/2kT}$$

$$B=7.3 \times 10^{15} [\text{cm}^{-3}\text{K}^{-3/2}]$$

$$E_g=1.12[\text{eV}] \text{ Electron Volt } 1\text{eV} = 1.6 \times 10^{-19} \text{ J}$$

$$k=8.62 \times 10^{-5} [\text{eV/K}]$$

$$\begin{aligned} p=n &= 7.3 \times 10^{15} (300^{3/2}) e^{-1.12/(2 \cdot 8.62 \times 10^{-5} \cdot 300)} \\ &= 1.5 \times 10^{10} \text{ carriers/cm}^3 \end{aligned}$$

There are 5×10^{22} atoms/cm³ for silicon, so only 1 out of every 5×10^{12} is ionized.

Current:

Free Electrons and Holes Moving.

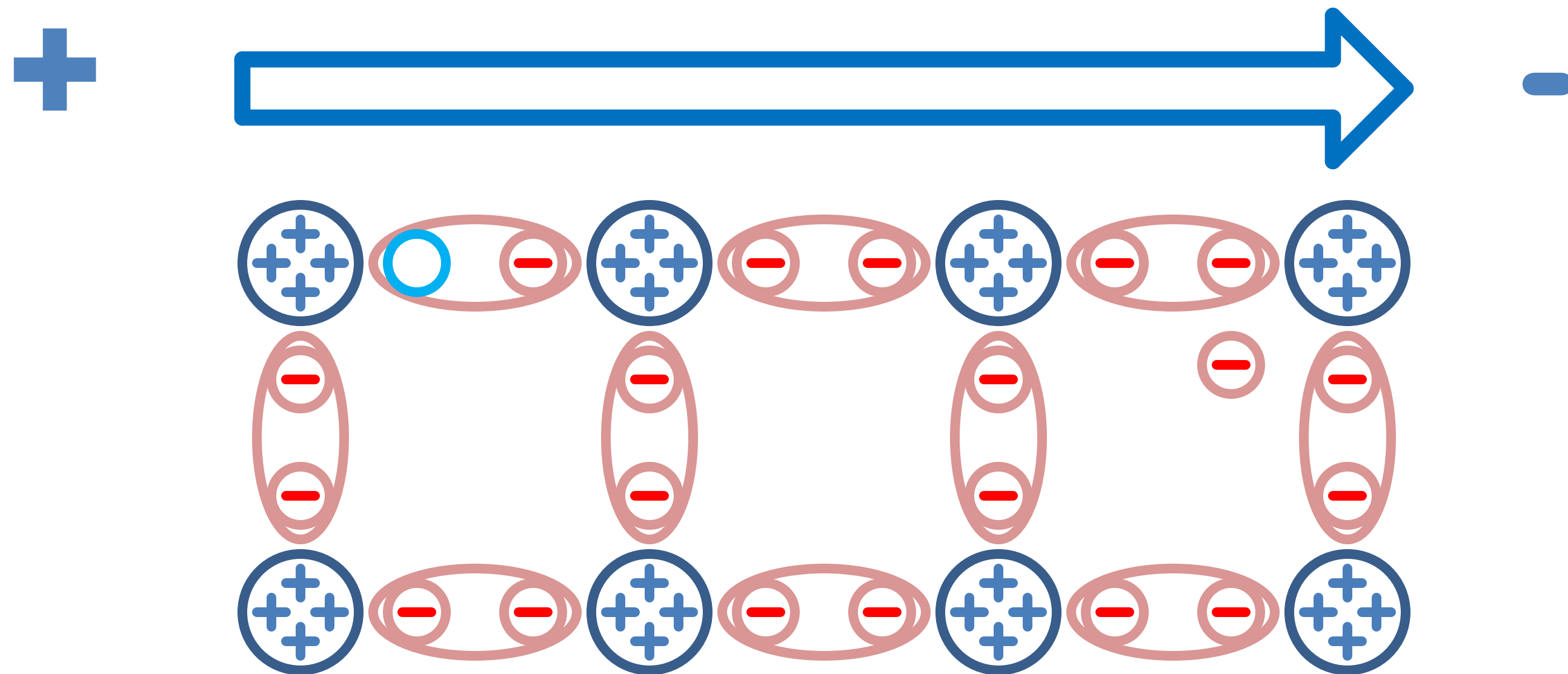
How do they move? (2 Types)

Currents:

Free Electrons and Holes Moving.

How do they move? (2 Types)

1) Apply an electric field (Voltage)

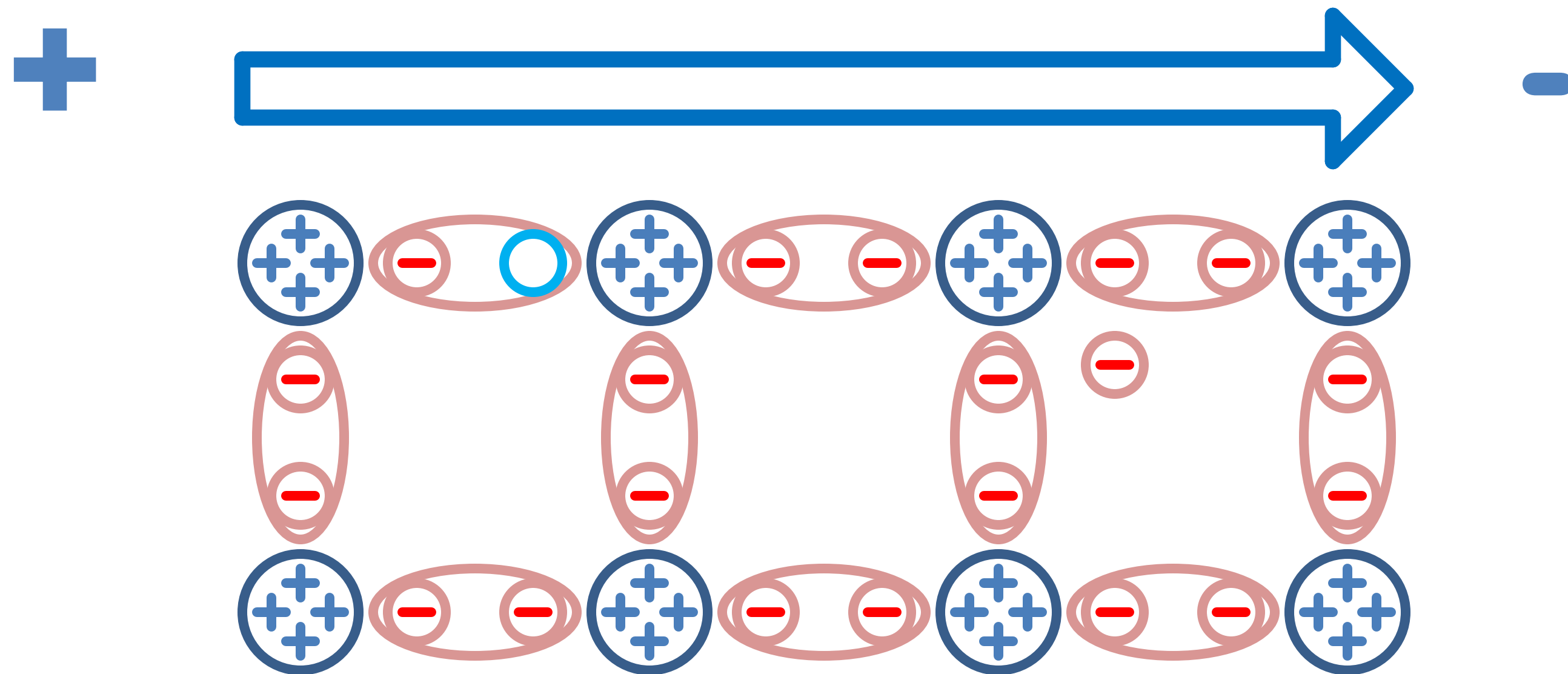


Currents:

Free Electrons and Holes Moving.

How do they move? (2 Types)

1) Apply an electric field (Voltage)

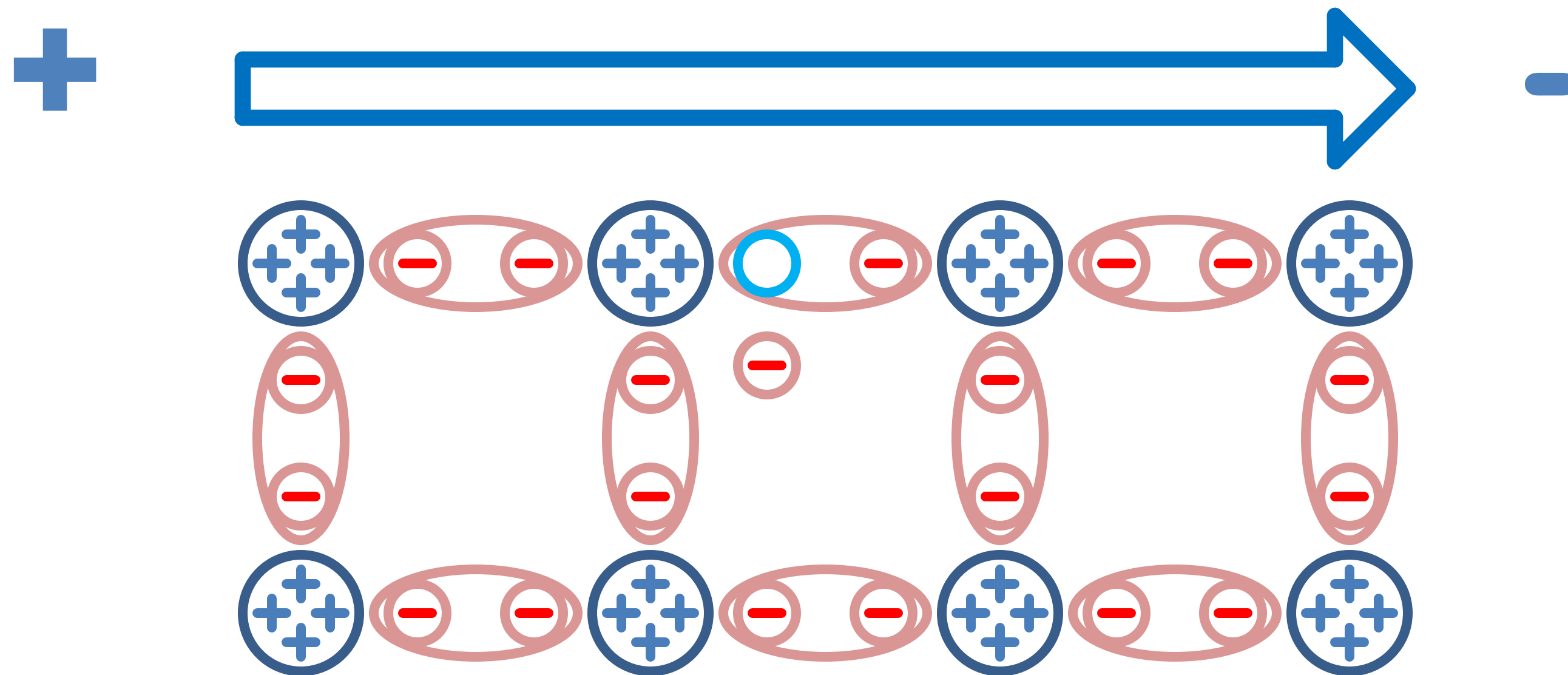


Currents:

Free Electrons and Holes Moving.

How do they move? (2 Types)

1) Apply an electric field (Voltage)

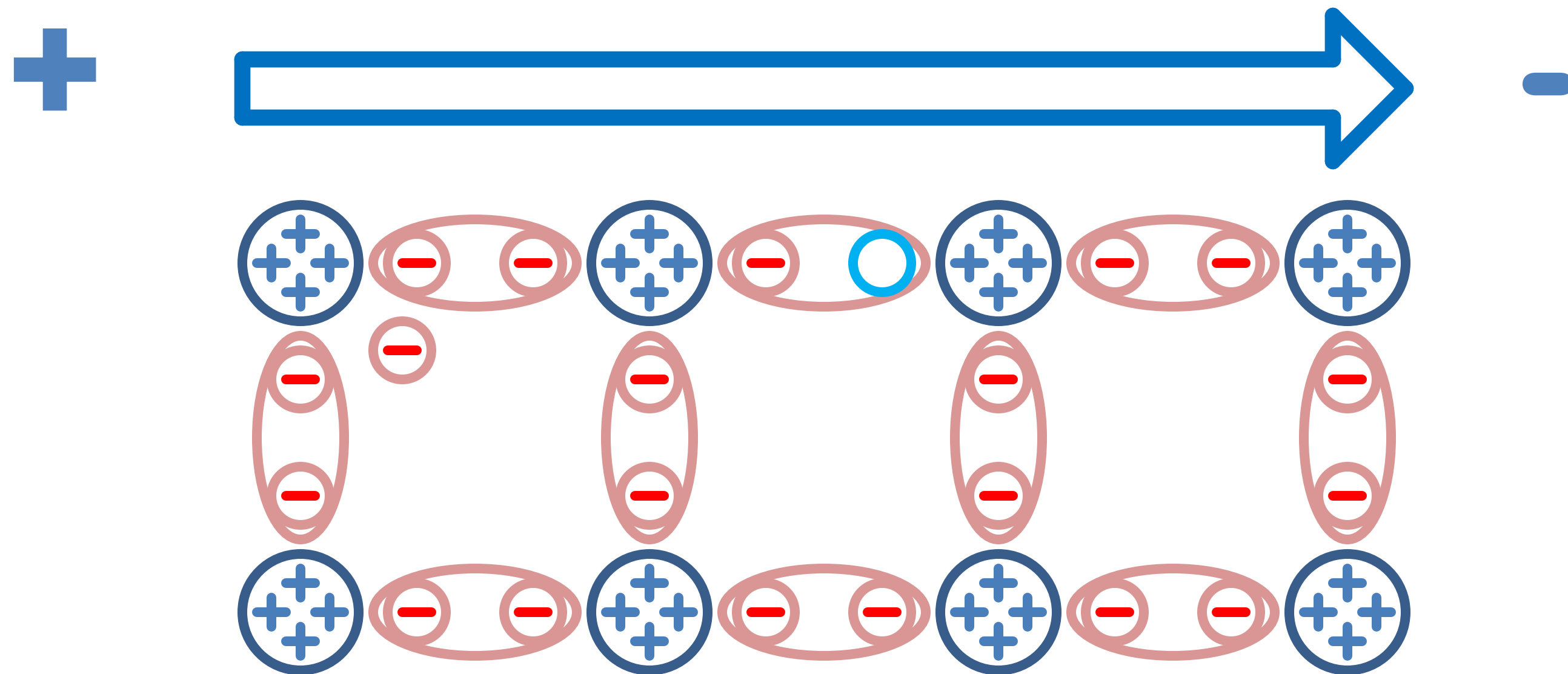


Currents:

Free Electrons and Holes Moving.

How do they move? (2 Types)

1) Apply an electric field (Voltage)



Drift Current: Current due to an e-field.

Force: Electric field (left to right)

Property: Charge

Equations:

velocity (cm/s) = mobility × Force (E=V/cm)

$v_{p\text{-drift}} = \mu_p E$ $\mu_p = 480 \text{ cm}^2/\text{Vs}$ (for silicon) depends on Temp

$v_{n\text{-drift}} = -\mu_n E$ $\mu_n = 1350 \text{ cm}^2/\text{Vs}$ (for silicon)

Current (A) = Area (cm²) × (#/cm³) × v (cm/s) × charge (q)

A = (#q)/s (left to right: same direction as E-field)

$I_p = A \cdot q \cdot p \cdot v_{p\text{-drift}} = A \cdot q \cdot p \cdot \mu_p \cdot E$

$I_n = -A \cdot q \cdot n \cdot v_{n\text{-drift}} = A \cdot q \cdot n \cdot \mu_n \cdot E$

Current Density = Current / Area = Conductivity × Force

$J_p = q \cdot p \cdot \mu_p \cdot E$ $J_n = q \cdot n \cdot \mu_n \cdot E$

$J = J_p + J_n = q(p \cdot \mu_p + n \cdot \mu_n)E = \sigma \cdot E$

Conductivity and resistivity

$\sigma = q(p \cdot \mu_p + n \cdot \mu_n)$ $\rho = 1/\sigma = 1/q(p \cdot \mu_p + n \cdot \mu_n)$

Drift Current: Current due to an e-field.

Force: Electric field (left to right)

Property: Charge

Conductivity and resistivity

$$\sigma = q(p \cdot \mu_p + n \cdot \mu_n) \quad \rho = 1/\sigma = 1/q(p \cdot \mu_p + n \cdot \mu_n)$$

What is the resistivity of intrinsic silicon at room temp (T=300K)?

Drift Current: Current due to an e-field.

Force: Electric field (left to right)

Property: Charge

Conductivity and resistivity

$$\sigma = q(p \cdot \mu_p + n \cdot \mu_n) \quad \rho = 1/\sigma = 1/q(p \cdot \mu_p + n \cdot \mu_n)$$

What is the resistivity of intrinsic silicon at room temp (T=300K)?

$$\rho = 1/\sigma = 1/q(p \cdot \mu_p + n \cdot \mu_n)$$

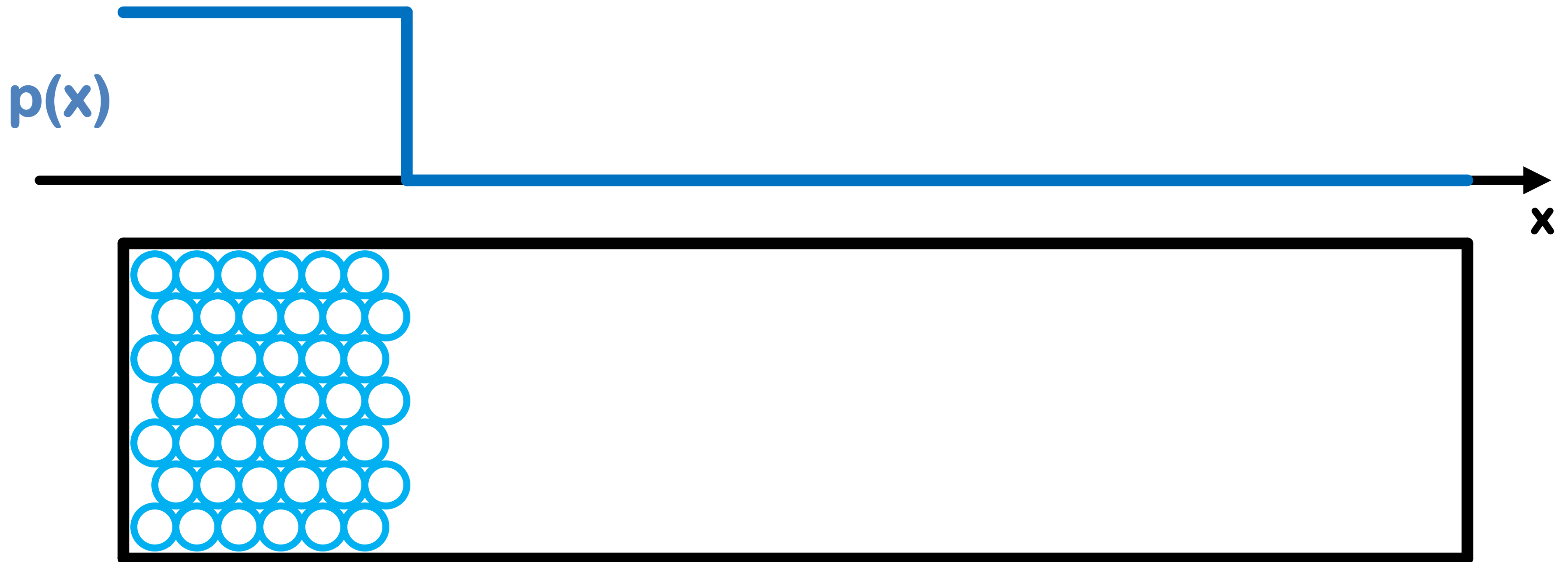
$$\rho = 1/(1.6e-19)(1.5e10 \cdot 480 + 1.5e10 \cdot 1350) = 2.28 \times 10^5 \, \Omega \, \text{cm}$$

Currents:

Free Electrons and Holes Moving.

How do they move? (2 Types)

2) Concentration Gradient, $p'(x)$

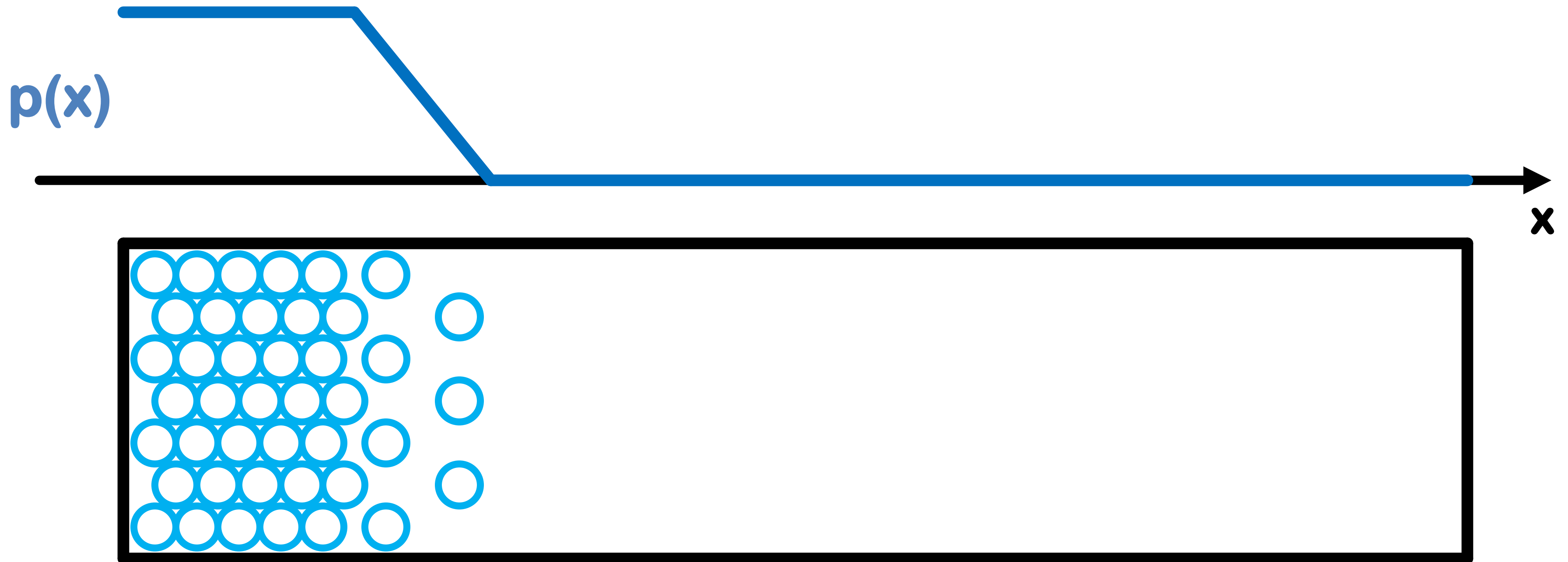


Currents:

Free Electrons and Holes Moving.

How do they move? (2 ways)

2) Concentration Gradient, $p'(x)$

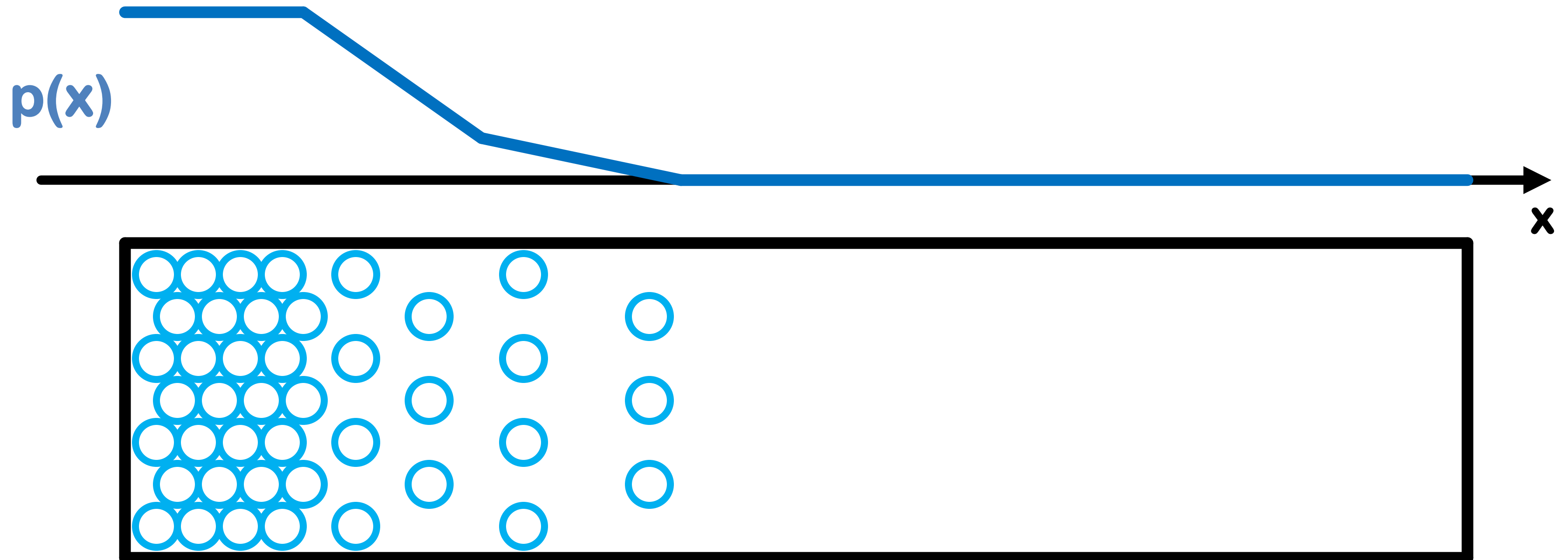


Currents:

Free Electrons and Holes Moving.

How do they move? (2 ways)

2) Concentration Gradient, $p'(x)$

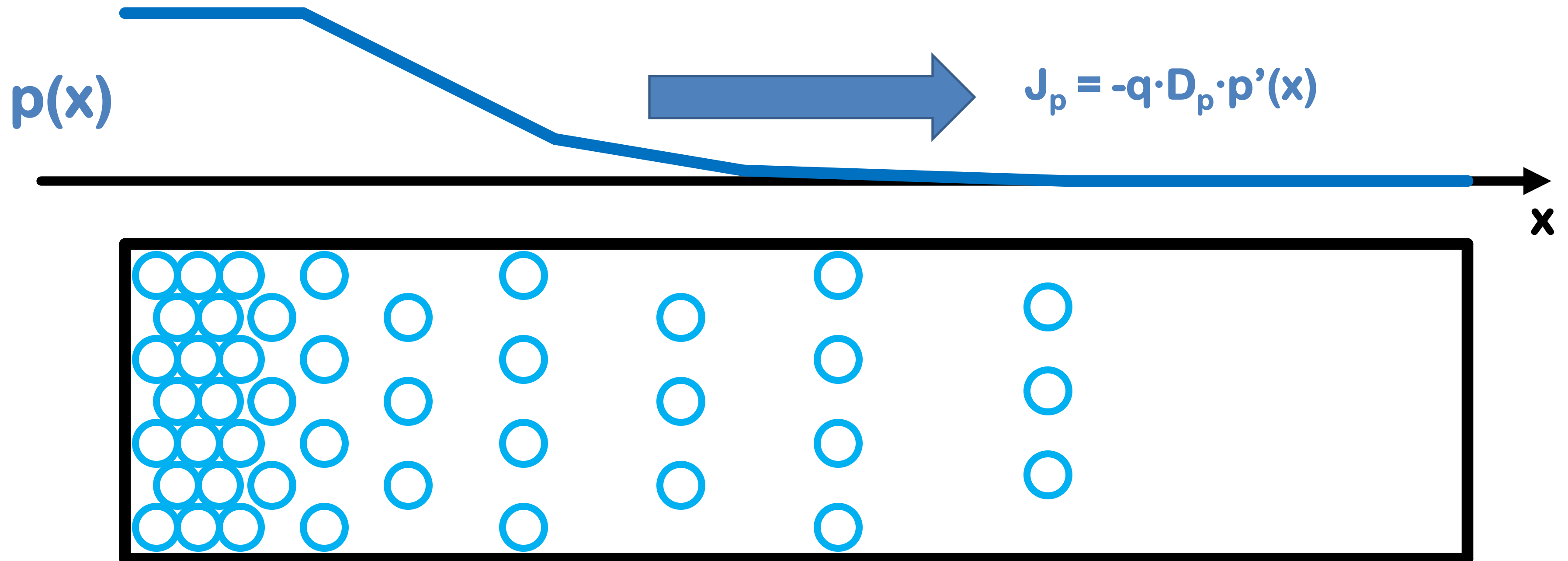


Currents:

Free Electrons and Holes Moving.

How do they move? (2 ways)

2) Concentration Gradient, $p'(x)$

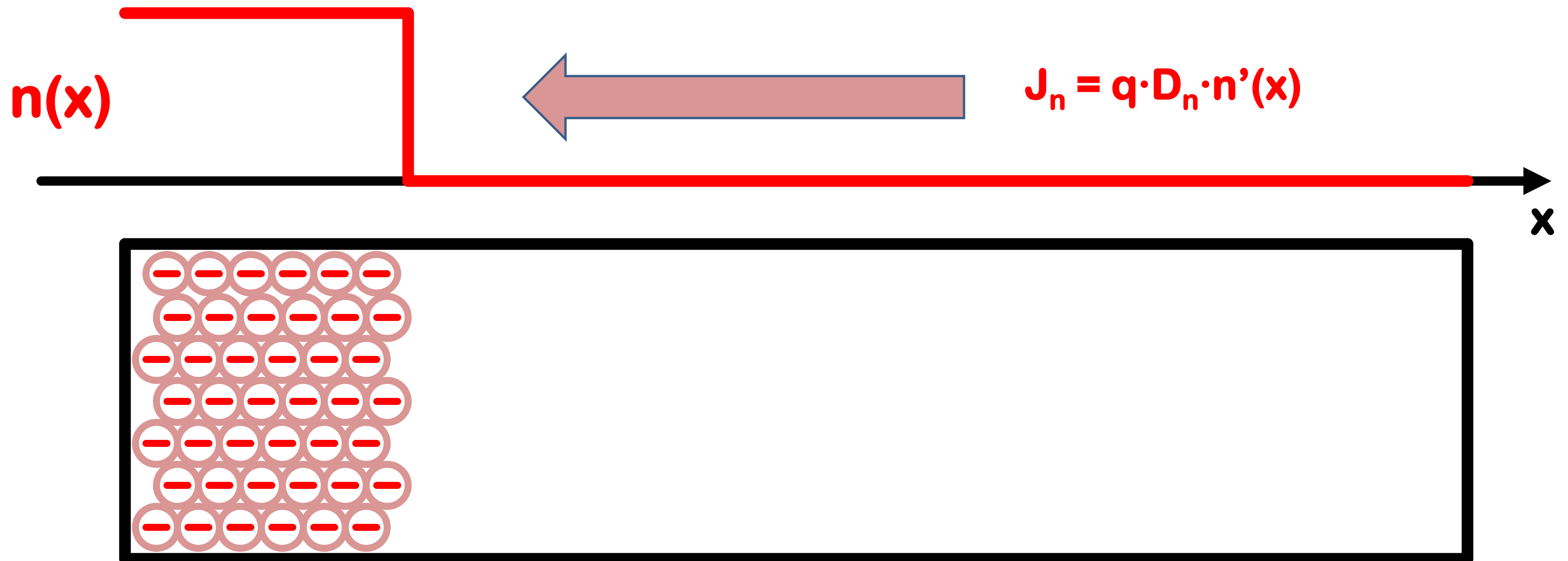


Currents:

Free Electrons and Holes Moving.

How do they move? (2 ways)

2) Concentration Gradient, $n'(x)$



Diffusion Current: Current due to an mass, heat, and con. grad.

Force: Heat

Property: Mass and Concentration Gradient

Current Density = Current / Area = Conductivity $\times$ Force

$$J_p = -q \cdot D_p \cdot p'(x) \quad D_p = 12 \text{cm}^2/\text{s} \quad (\text{for silicon})$$

$$J_n = q \cdot D_n \cdot n'(x) \quad D_n = 35 \text{cm}^2/\text{s} \quad (\text{for silicon})$$

Remember, Current = Current Density $\times$ Area

$$I_p = -A \cdot q \cdot D_p \cdot p'(x)$$

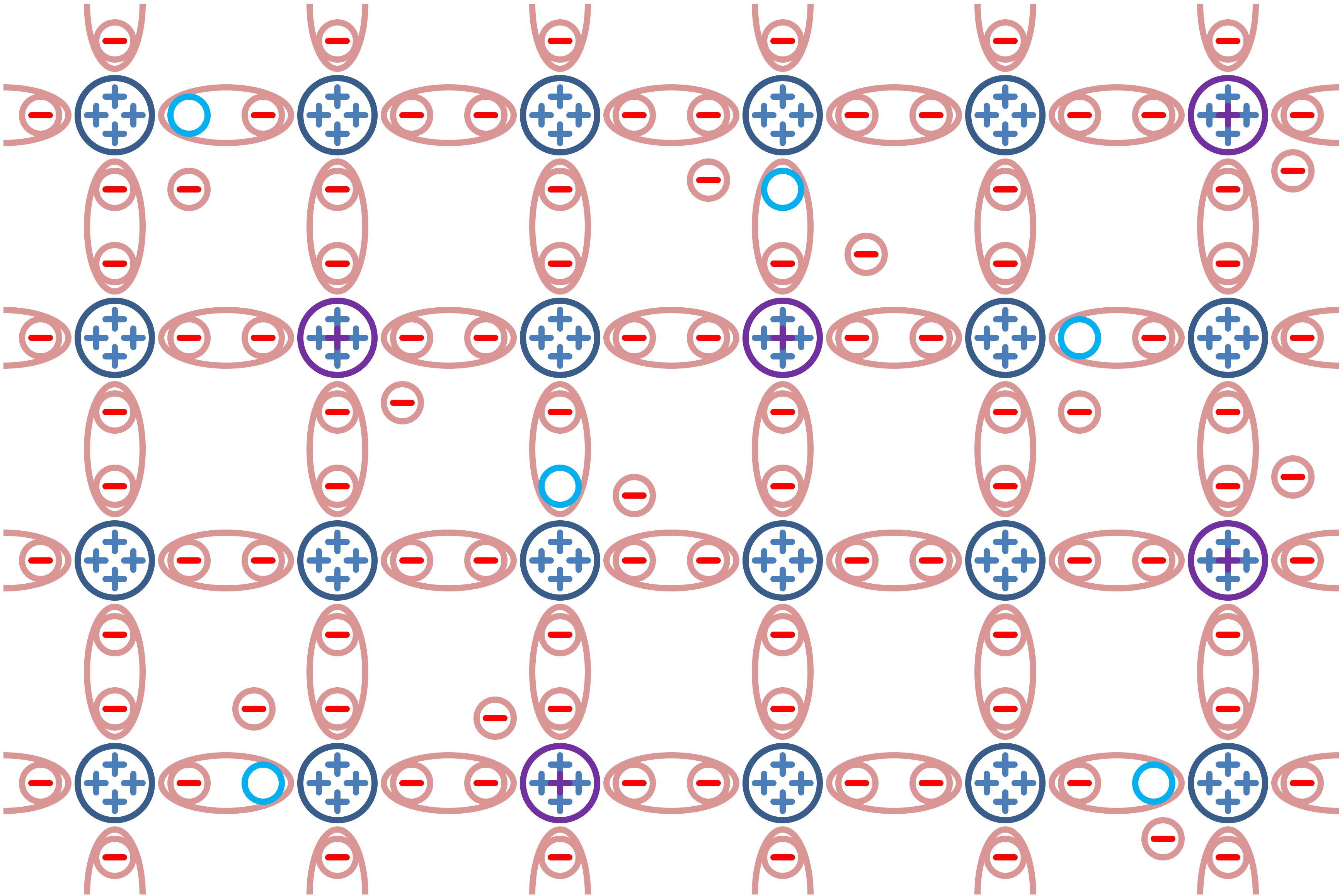
$$I_n = A \cdot q \cdot D_n \cdot n'(x)$$

$$D_n / \mu_n = D_p / \mu_p = V_T$$

The problem with pure (intrinsic) silicon is that p and n are small resulting in a poor conductor.

How can we increase the number of f.e. or holes?

Doped Silicon: With Phosphorus (15)



N-type Silicon:

Doped with **Phosphorus (Donor)**

Excess of free electrons (negative)

$n_n = N_D$ Donor Concentration

$n_n \gg p_n$

$p_n n_n = n_i^2$

$p_n = n_i^2 / N_D$

$p = n_i^2 / N_D$



Charge Carriers

free electrons:

majority carriers

holes:

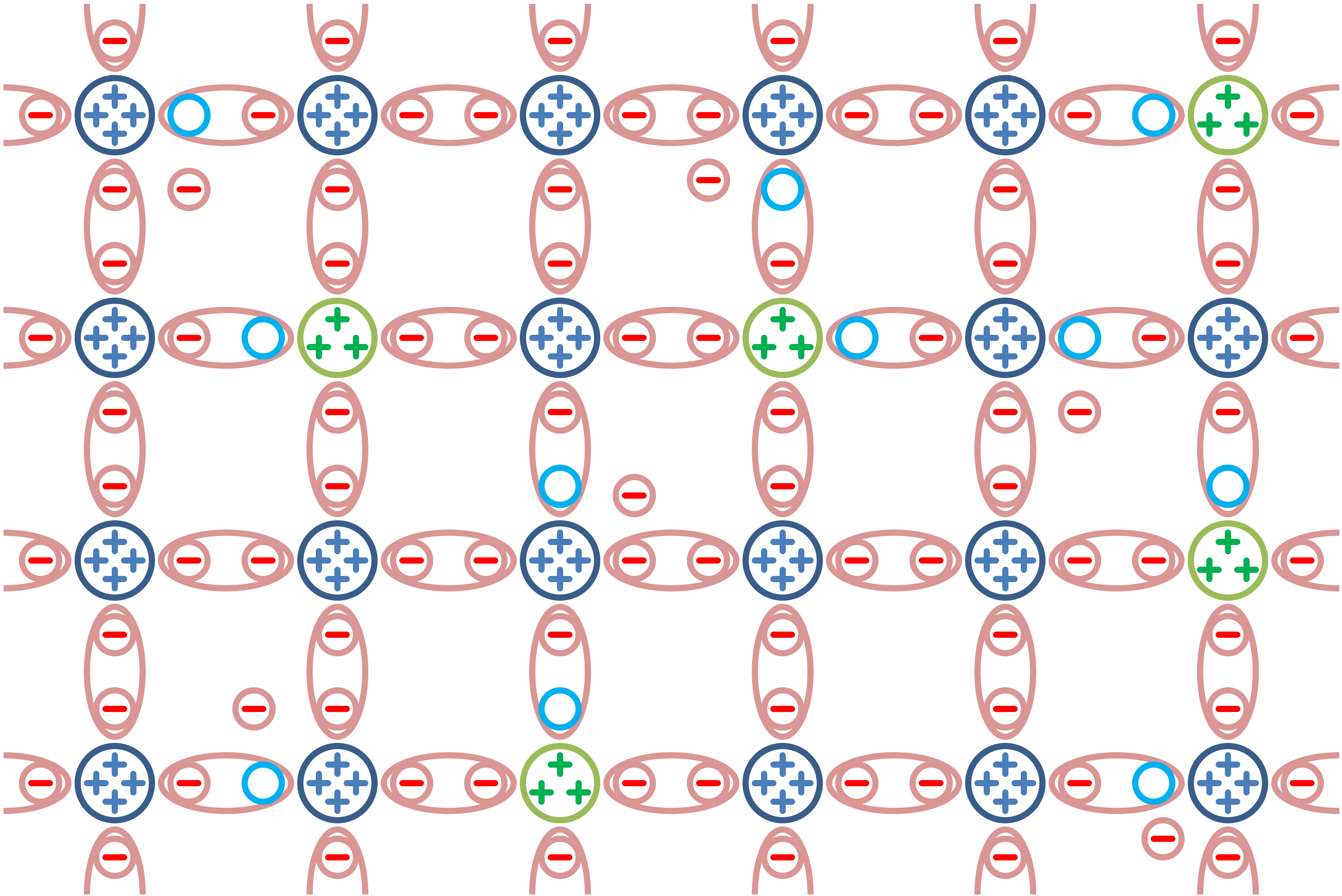
minority carriers

If f.e. are removed to equalize holes and f.e.

The region becomes depleted (poor cond.)

The region becomes positively charged

Doped Silicon: With Boron (5)



P-type Silicon:

Doped with **Boron (Acceptor)**

Excess of holes (positive)

$p_p = N_A$ Donor Concentration

$p_p \gg n_p$

$p_p n_p = n_i^2$

$n_p = n_i^2 / N_A$

Charge Carriers

holes:

majority carriers

free electrons:

minority carriers

If holes are filled to equalize holes and f.e.

The region becomes depleted (poor cond.)

The region becomes negatively charged

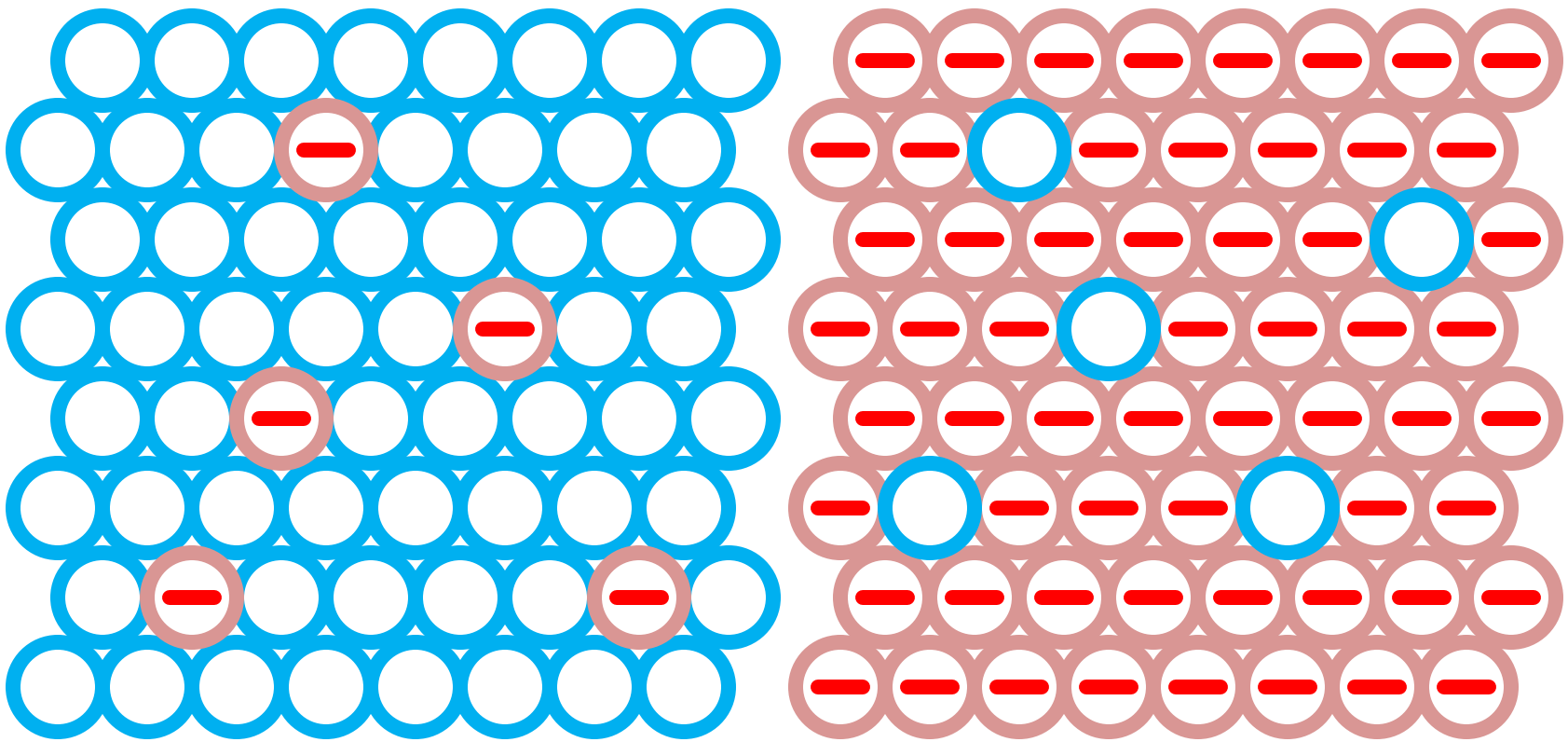
Review (Silicon):

- Silicon lattice (intrinsic, covalent bonds).
 - 0K – no charge carriers.
 - >0K – free electrons (negative), holes (positive).
 - n : concentration of free electrons.
 - p : concentration of holes.
 - $p=n=n_i$ which is a function of Temperature.
- Current (two types)
 - Drift – charge moving due to electric field.
 - Diffusion – charge moving due to heat and concentration gradient.
- Intrinsic silicon even at room temperature does not have a sufficient amount of charge carriers to be a good conductor

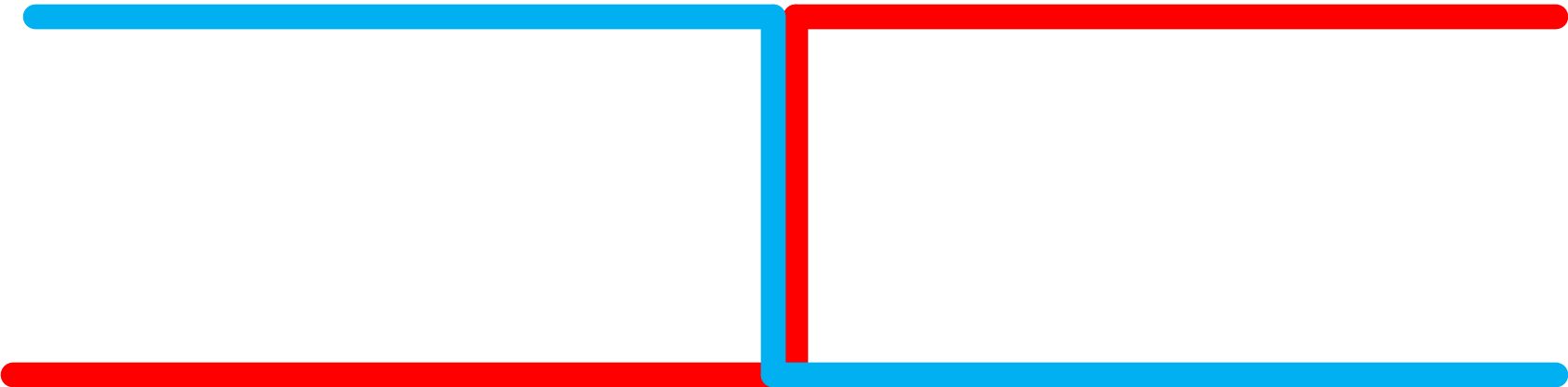
Review (Doped Silicon):

- **N-Type: use Phosphorus to add extra electrons.**
 - **Majority carriers: f.e. – $n_n = N_D$**
 - **Minority carriers: holes – $p_n = n_i^2 / N_D$**
 - **Depleted**
 - **Remove f.e. to equalize n and p.**
 - **Results in a positive charge.**
- **P-Type: use Boron to add extra holes.**
 - **Majority carriers: holes – $p_p = N_A$**
 - **Minority carriers: f.e. – $n_p = n_i^2 / N_A$**
 - **Depleted**
 - **Add f.e. to fill holes and equalize n and p.**
 - **Results in a negative charge.**

The PN Junction:



$n(x), p(x)$



Diffusion Current

Net Charge

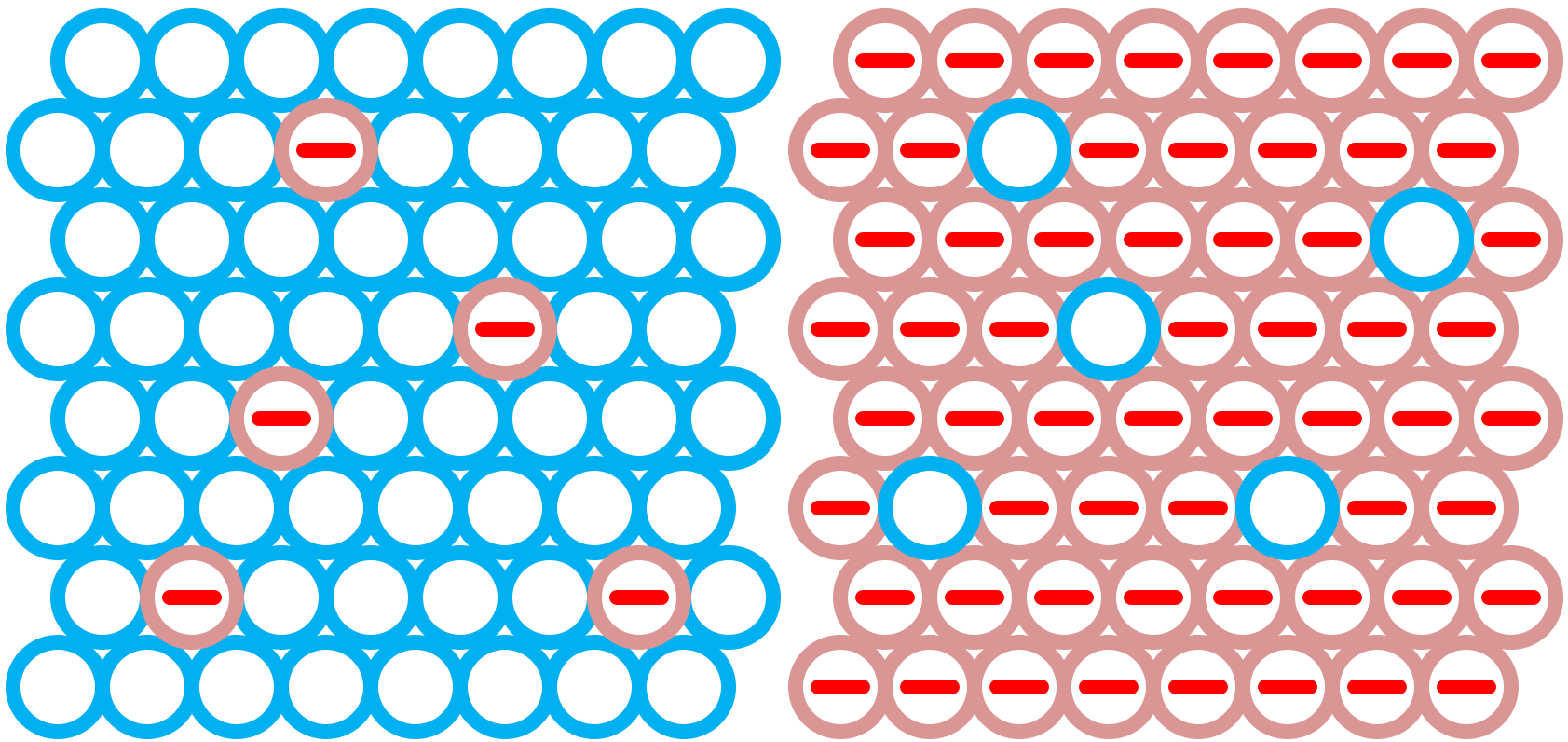


E-field

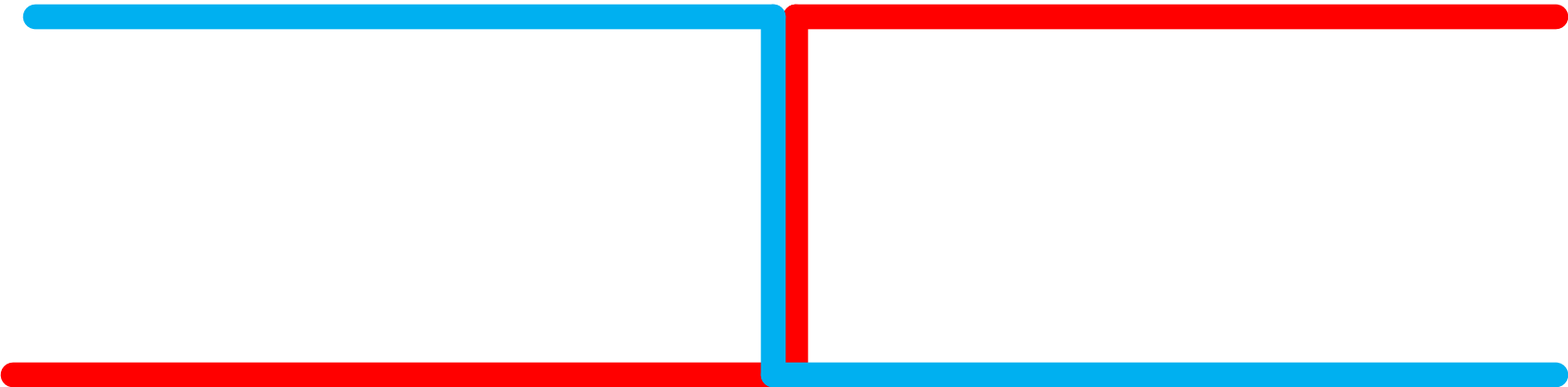
NONE

Drift Current

The PN Junction:



$n(x), p(x)$



Diffusion Current



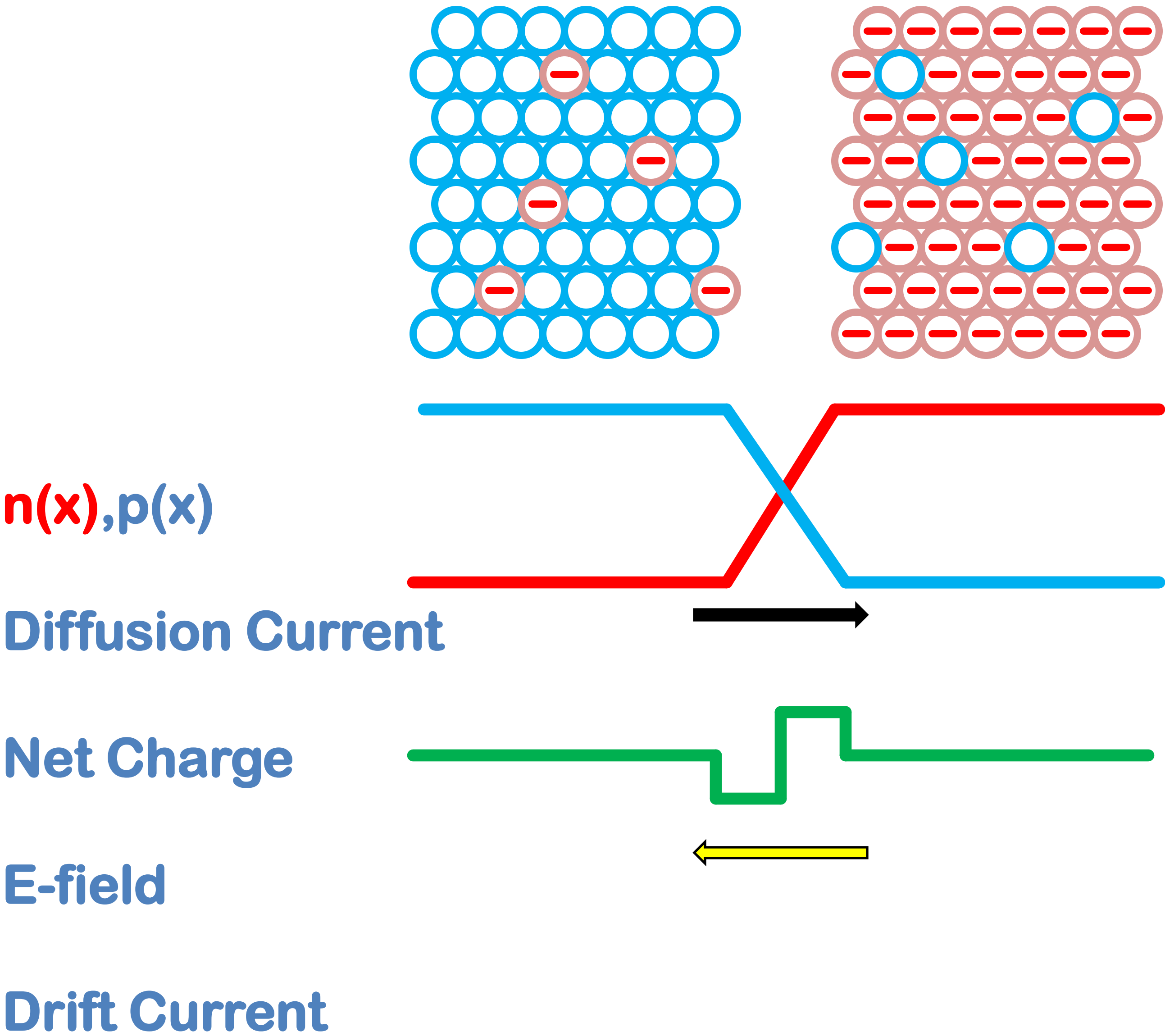
Net Charge



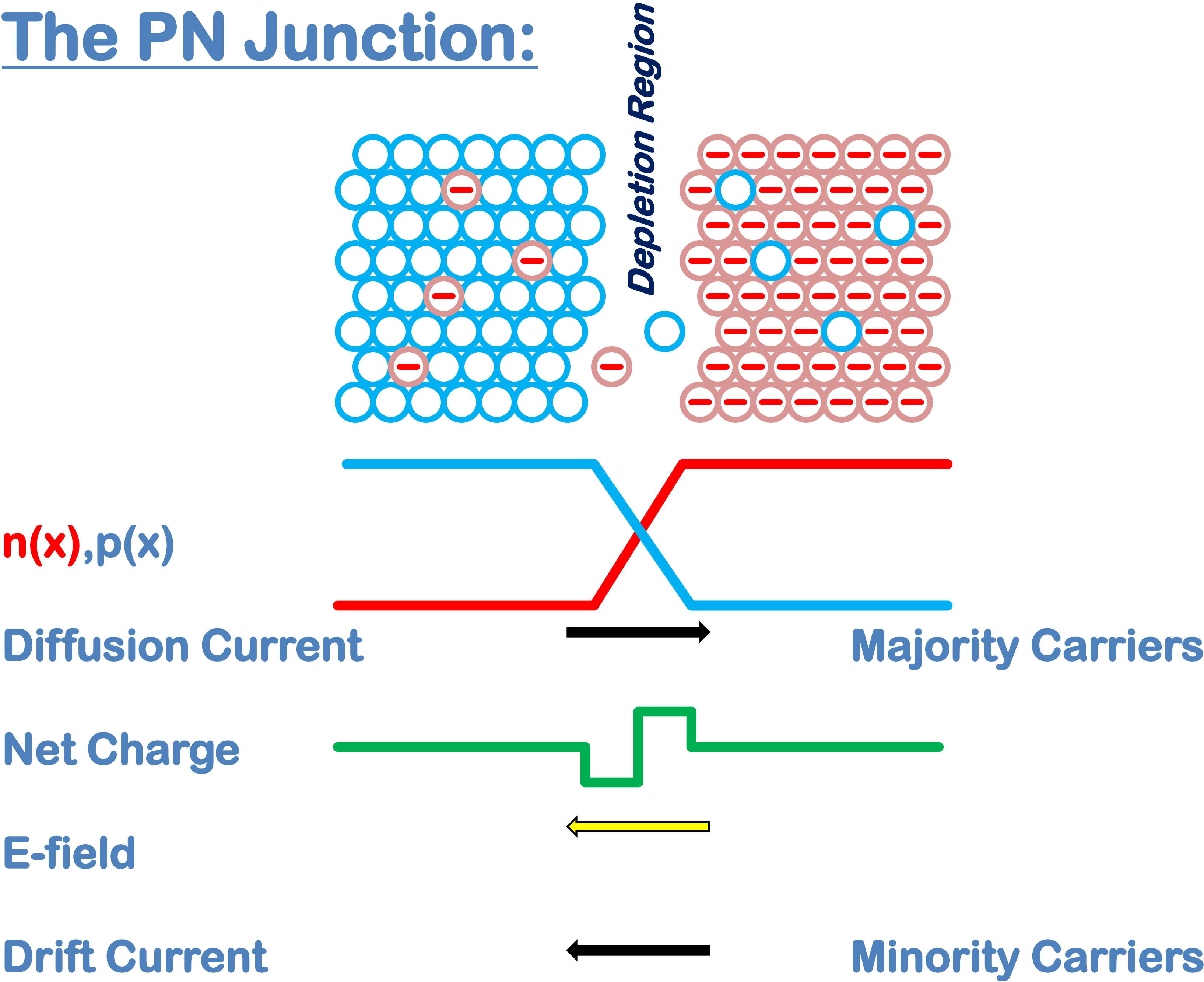
E-field

NONE

The PN Junction:



The PN Junction:



The PN Junction:

Diffusion Current (anode to cathode)

Majority Carriers

Significantly blocked by the depletion region voltage.

Dependent on voltage (overcome the depletion region voltage).

Drift Current (cathode to anode)

Minority Carriers

Not dependent on e-field, but rather the small number of available charge carrier.

Significantly reduced by small number of minority carriers.

Relatively constant.

Diffusion and Drift Currents are in opposite directions.

$$i_D = i_{\text{Diffusion}} - i_{\text{Drift}}$$

The PN Junction:

Diffusion Current

Majority Carriers

Significantly blocked by the depletion region voltage.

Dependent on voltage (overcome the depletion region voltage).

Drift Current

Minority Carriers

Not dependent on e-field, but rather the small number.

Significantly reduced by small number of minority carriers.

Relatively constant.

Forward Biased PN Junction.

v_D is from P to N, opposite that of the depletion region voltage.

Diffusion current increases.

The solution to a diffusion equation is an exponential.

$$i_{\text{diffusion}} = K \exp(v_D/nV_T)$$

The PN Junction:

Diffusion Current

Majority Carriers

Significantly blocked by the depletion region voltage.

Dependent on voltage (overcome the depletion region voltage).

Drift Current

Minority Carriers

Not dependent on e-field, but rather the small number.

Significantly reduced by small number of minority carriers.

Relatively constant.

Reversed Biased PN Junction.

v_D is from N to P, enhances that of the depletion region voltage.

Diffusion current is pushed to near zero.

Drift current is constant.

$$i_{\text{drift}} = I_S$$

The PN Junction:

Diffusion Current

Majority Carriers

Significantly blocked by the depletion region voltage.

Dependent on voltage (overcome the depletion region voltage).

Drift Current

Minority Carriers

Not dependent on e-field, but rather the small number.

Significantly reduced by small number of minority carriers.

Relatively constant.

Diffusion and Drift Currents are in opposite directions.

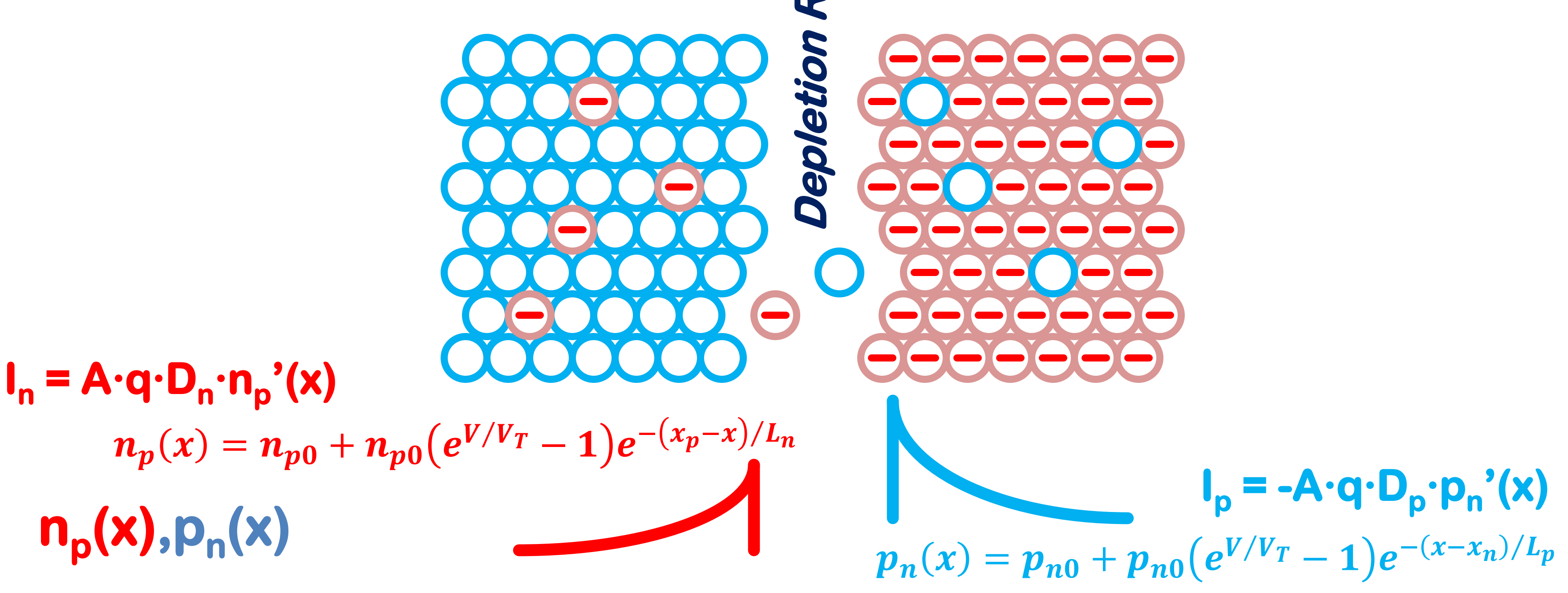
$$i_D = K \exp(v_D/nV_T) - I_S$$

Passive device $i_D(0) = 0$, so $K = I_S$.

$$i_D = I_S(\exp(v_D/nV_T) - 1)$$

The PN Junction:

$$I_S = Aqn_i^2 \left(\frac{D_p}{L_p N_D} + \frac{D_n}{L_n N_A} \right)$$



Diffusion Current → Majority Carriers



E-field ←

Drift Current ← Minority Carriers

The PN Junction:

Diffusion Current

Majority Carriers

Significantly blocked by the depletion region voltage.

Dependent on voltage (overcome the depletion region voltage).

Drift Current

Minority Carriers

Not dependent on e-field, but rather the small number.

Significantly reduced by small number of minority carriers.

Relatively constant.

PN Junction in Breakdown.

V_D is from N to P and is very large.

V_D is sufficiently large (negative) to break covalent bonds (Zener).

Rush of free electrons.

Electrons collide with other bonds freeing those electrons
(Avalanche).